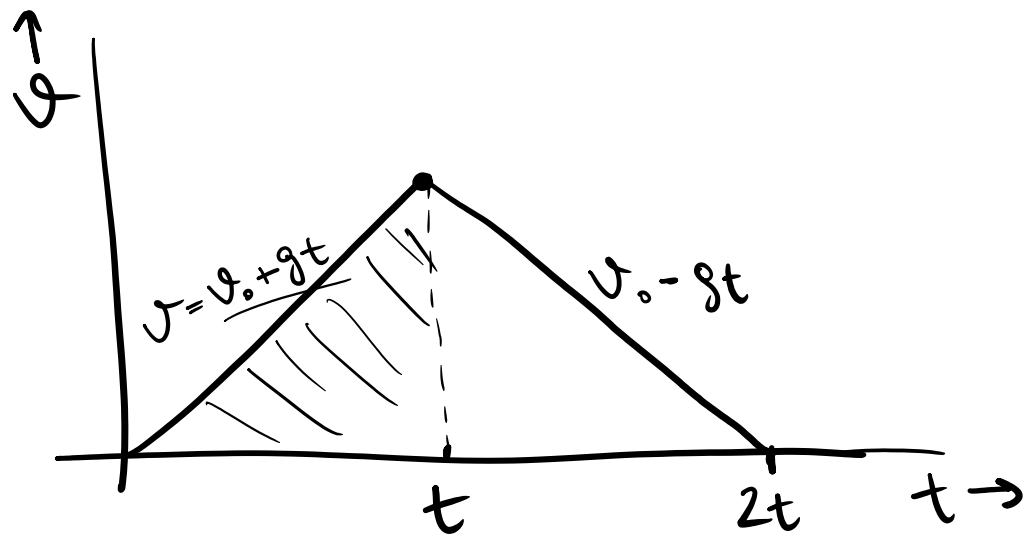


$$\text{Average velocity} = \frac{\int v \cdot dt}{\int dt} = \frac{\int v dt}{t}$$

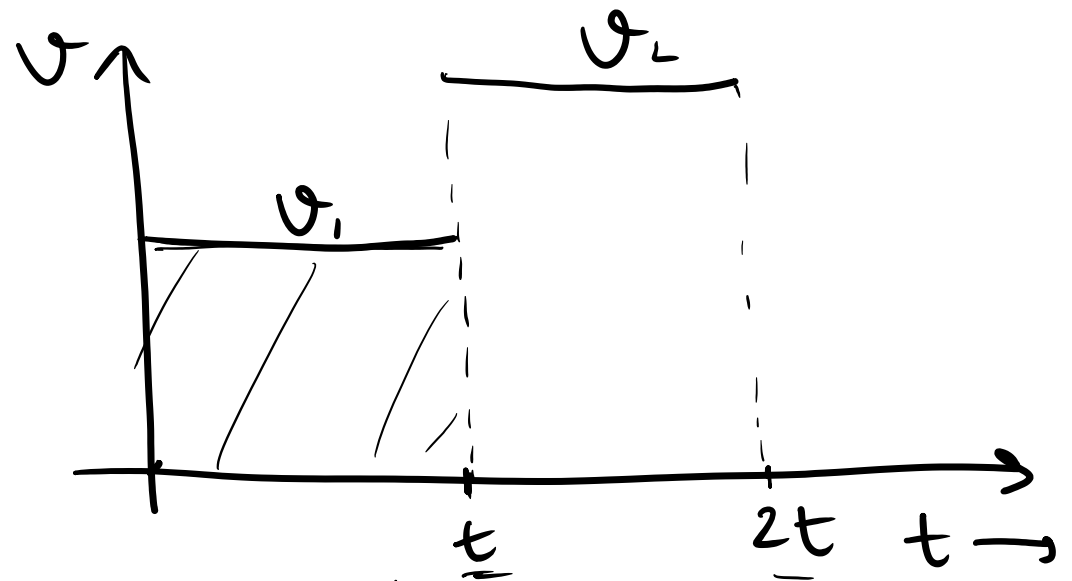
$$\text{Average} = \frac{\int f(t) \cdot dt}{\int dt} = \frac{\int f(t) dt}{t}$$



$$\underline{f(t)} = \underline{t^2} + \underline{2t} + \underline{5}$$



$$\frac{\int_0^t (v_0 + gt) \cdot dt}{\int_0^t dt} + \frac{\int_t^{2t} (v_0 - gt) \cdot dt}{\int_t^{2t} dt}$$



$$\begin{aligned} v_{av} &= \frac{\int v dt}{\int dt} \\ &= \frac{\int_0^t v_1 dt + \int_t^{2t} v_2 dt}{t]_0^{2t}} \\ &= \frac{v_1 t]_0^t + v_2 t]_t^{2t}}{2t - 0} \\ &= (v_1 + v_2) / 2 \end{aligned}$$

$$v = 4t^3 - 2t$$

$$\frac{dv}{dt} = \underline{12t^2 - 2} = a = 12(2) - 2 = 22 \text{ m/s}^2$$

$$\int v dt = \int 4t^3 dt - \int 2t dt$$

$$s \Big|_0^2 = t^4 - t^2$$

$$2 = t^4 - t^2 = \underline{t^2(t^2 - 1) = 2}$$

$$\text{Let } t^2 = y$$

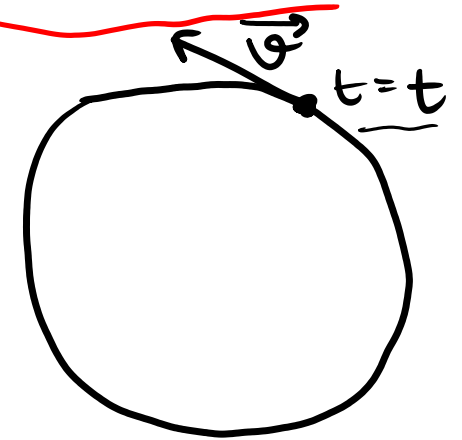
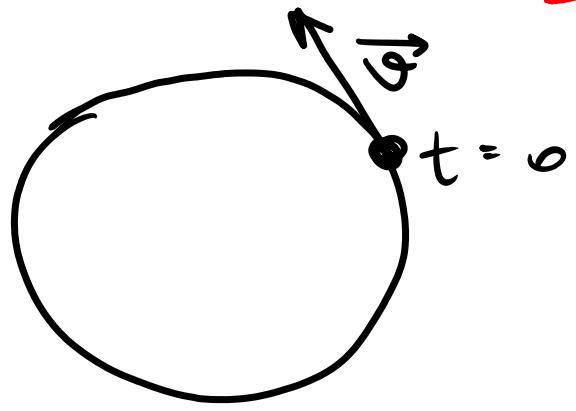
$$y(y-1) = 2$$

$$\underline{y = 2}$$

$$t^2 = 2$$

$$t = \sqrt{2}$$

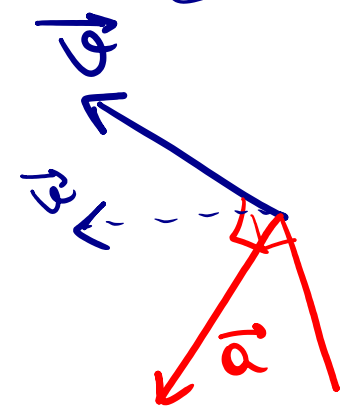
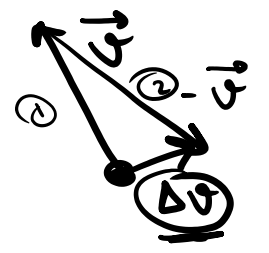
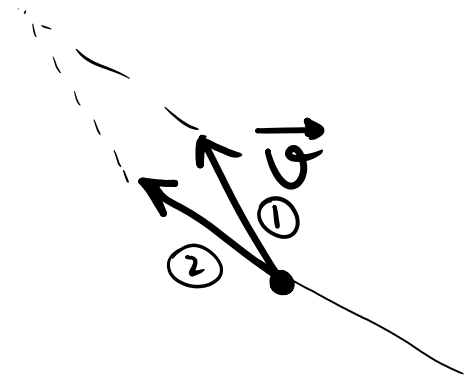
Circular Motion



$|\vec{v}| = \text{Same}$

$\frac{d\vec{v}}{dt} = \vec{a} = \frac{v^2}{r} (\perp)$ Centripetal acceleration

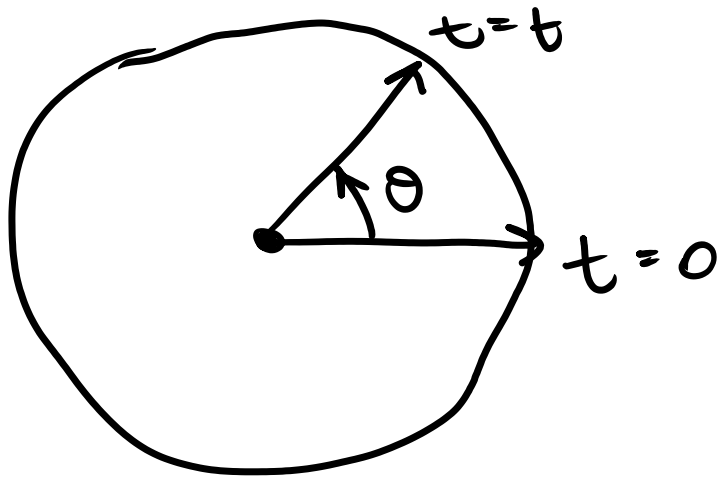
Changing direction



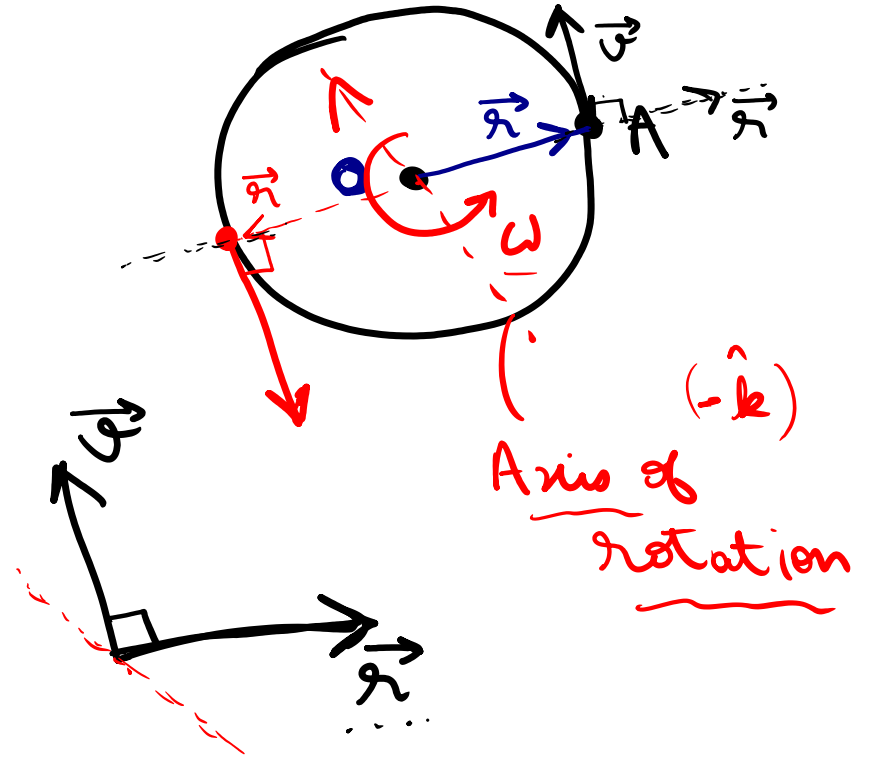
$$\vartheta = r\omega$$

$$\omega = \vartheta / r$$

Angular velocity



$$\vec{v} = \vec{r} \times \vec{\omega}$$



Linear

s

v

a

$$v^2 - u^2 = 2as$$

Circular

θ

ω

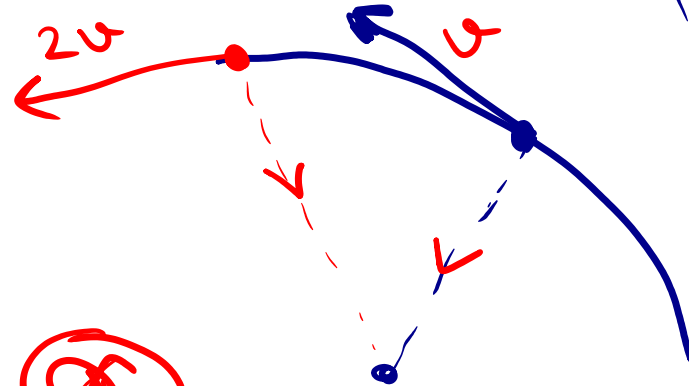
α

$$l = r\theta$$

$$\frac{dl}{dt} = r \frac{d\theta}{dt}$$

$$v = r\omega$$
$$a = r\alpha$$

$$\omega_f^2 - \omega_i^2 = 2\alpha\theta$$



$$a_c = \frac{v^2}{r}$$
$$= \omega^2 r$$

$$\omega_f - \omega_i = \alpha t$$

\perp to v

Newton's Law

$$\underline{\sum \vec{F}_{\text{ext}}} = m \underline{\vec{a}_{\text{net}}}$$

⇒



Action - reaction pairs
always ACT ON DIFFERENT
BODIES

FBD

1) Define your frame of reference. Define your system

- i) m
- ii) M
- iii) $(m+M)$

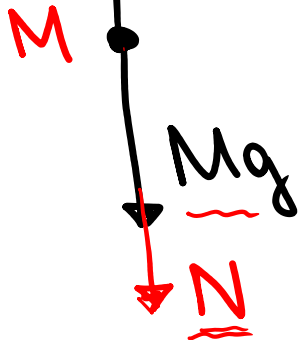
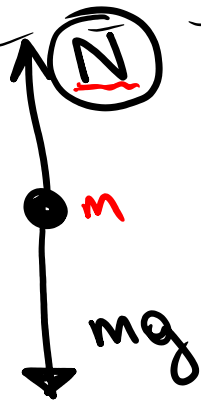


Earth

$$\sum F_{ext} = 0$$

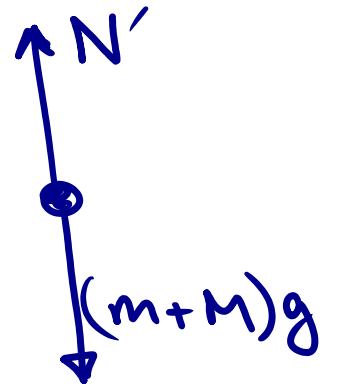
$$N - mg = 0$$

$$\underline{N = mg}$$

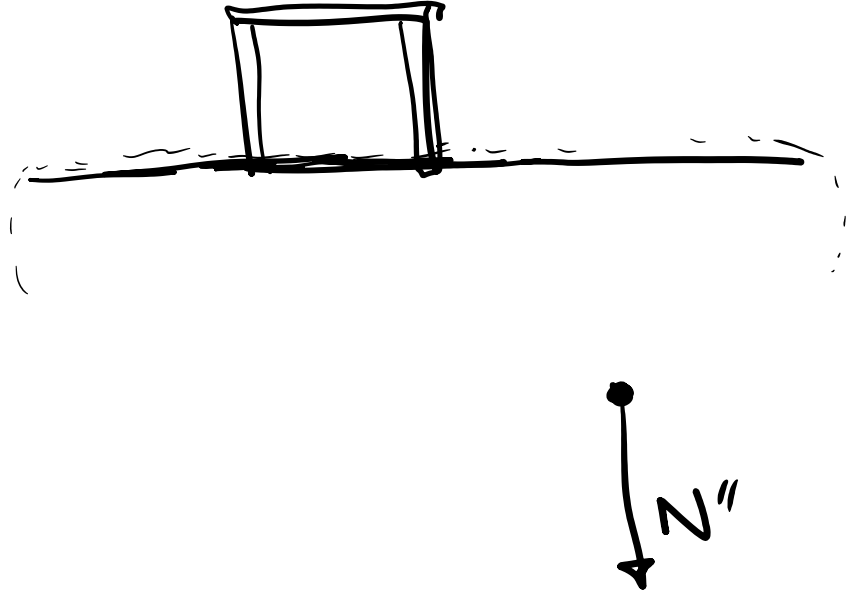


$$N + Mg - N' = 0$$

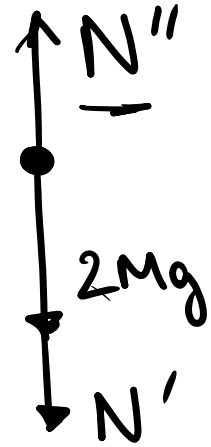
$$\underline{mg + Mg = N'}$$



$$N' = (m+M)g$$



FBD of the Table



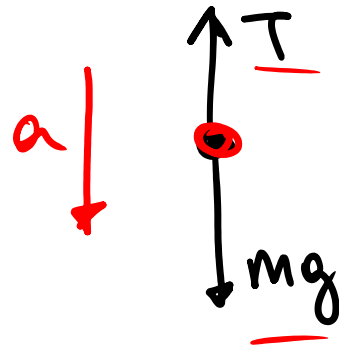
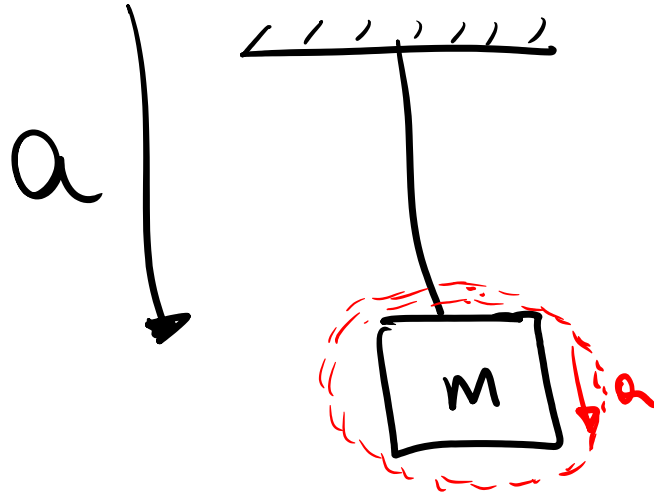
$$N'' = 2mg + N'$$

$$= 2mg + mg + Mg$$

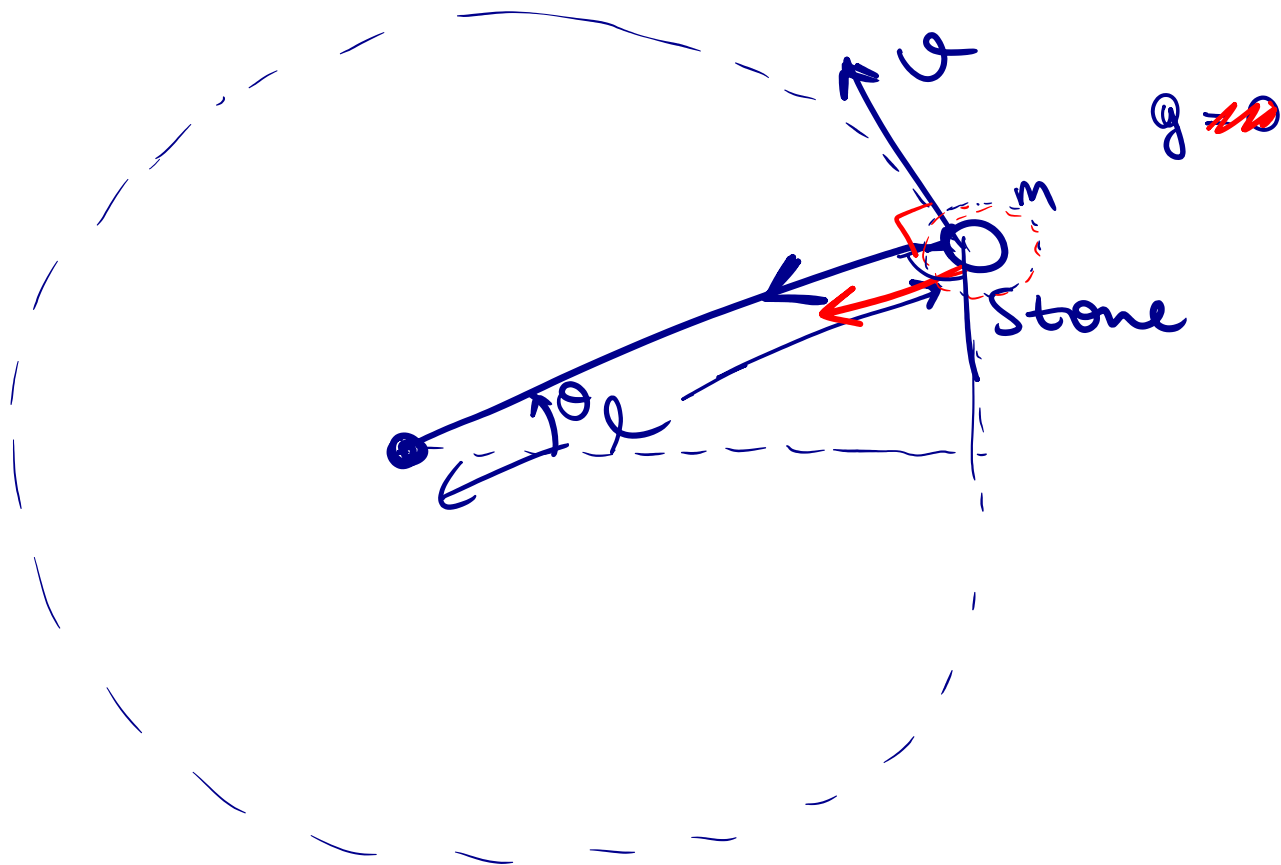
NORMAL \perp to
 PUSH FORCE
 Surface

Tension force

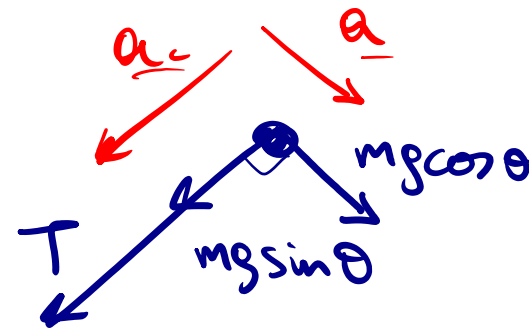
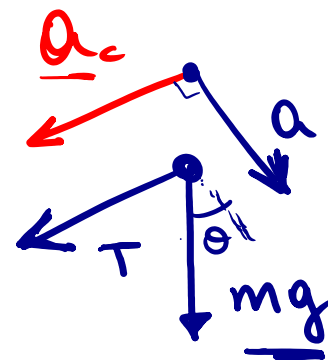
PULLING FORCE



$$\begin{aligned} \Sigma F_{\text{net}} &= m a_{\text{net}} \\ \hline mg - T &= ma \end{aligned}$$

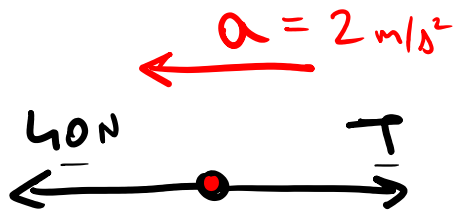
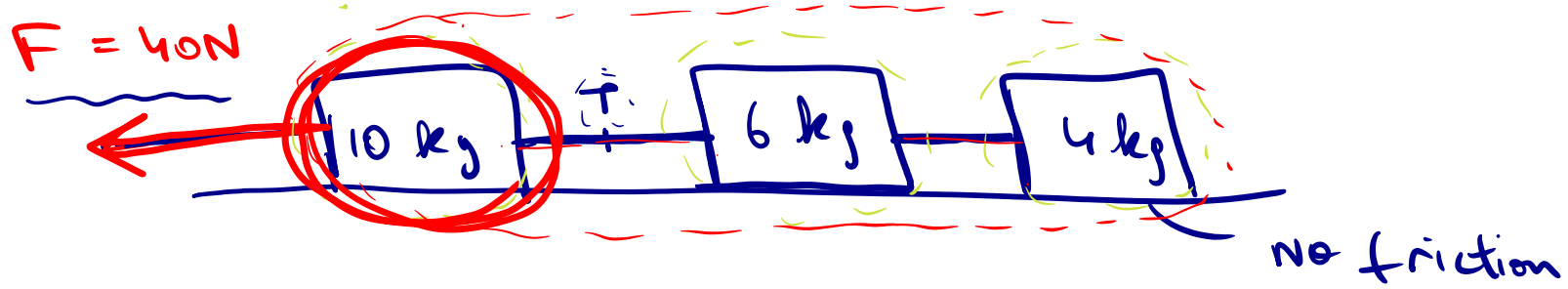


$$a_c = \frac{v^2}{r}$$



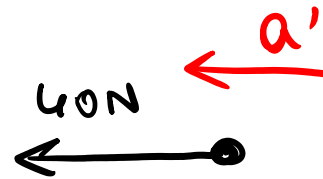
$$T + mg \sin \theta = m \frac{v^2}{r}$$

$$mg \cos \theta = ma$$



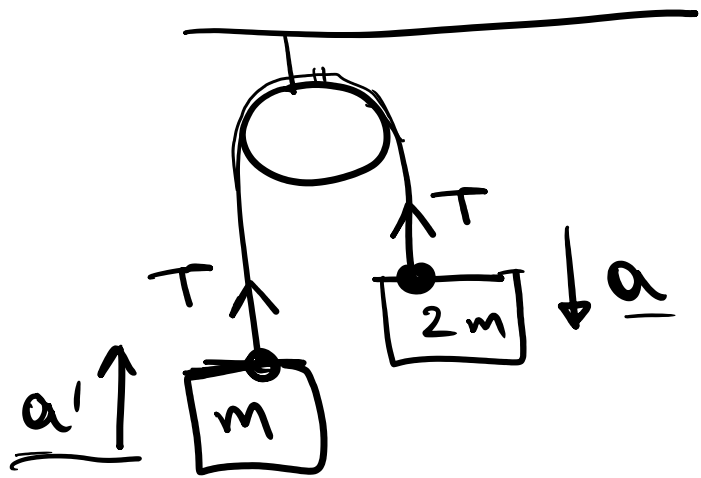
$$40 - T = 20$$

$$T = 20$$



$$40 = (20)a'$$

$$a' = 2\text{ m/s}^2$$



$$\vec{T} \cdot \vec{a}' + \vec{T} \cdot \vec{a} = 0$$

$$T a' - T a = 0$$

$$\boxed{a = a'}$$

$$\begin{aligned} \sum F &= 0 \\ T &= T \end{aligned} \quad m=0$$

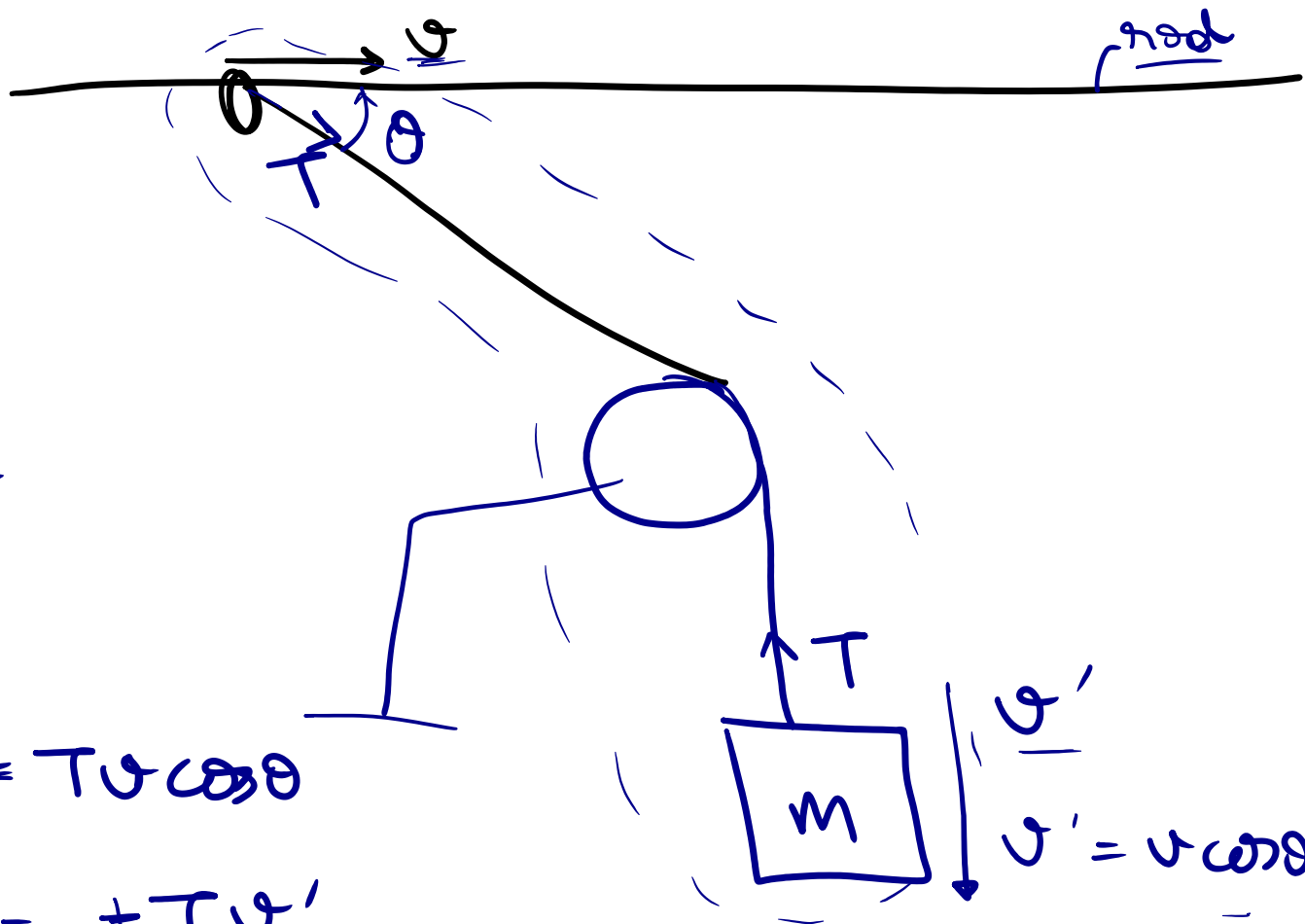
$$\sum \underline{T \cdot a} = \underline{0} \quad \checkmark$$



$$\sum T \cdot \checkmark = 0$$

$$T \cdot \checkmark = 0$$

$$T \cdot \checkmark = 0$$



Relationship?
 v' & v

v

v'

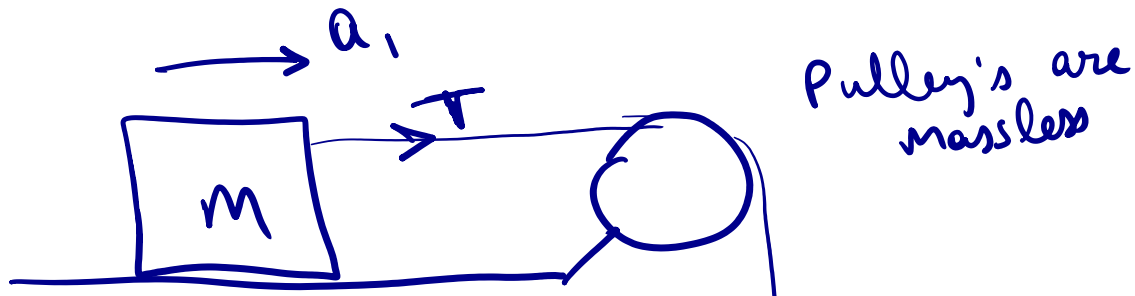
$$\underline{T \cdot v} = T v \cos \theta$$

$$T \cdot v' = +T v'$$

$$T v \cos \theta + T v' = 0$$

$$\underline{-v \cos \theta = v'}$$

$$v' = v \cos \theta$$

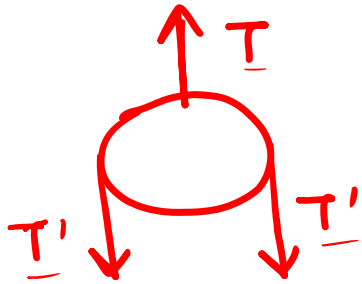


a_1, a_2, a_3

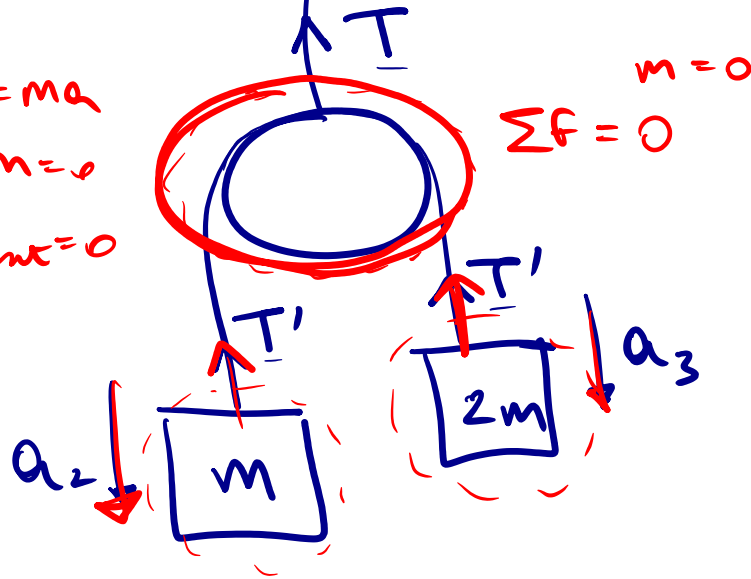
$$\underline{\underline{\sum \vec{T} \cdot \vec{a} = 0}}$$

Relation

$$\begin{aligned} \sum F_{\text{ext}} &= ma \\ m &= 0 \\ \sum F_{\text{ext}} &= 0 \end{aligned}$$



$$\underline{\underline{2T' = T}}$$

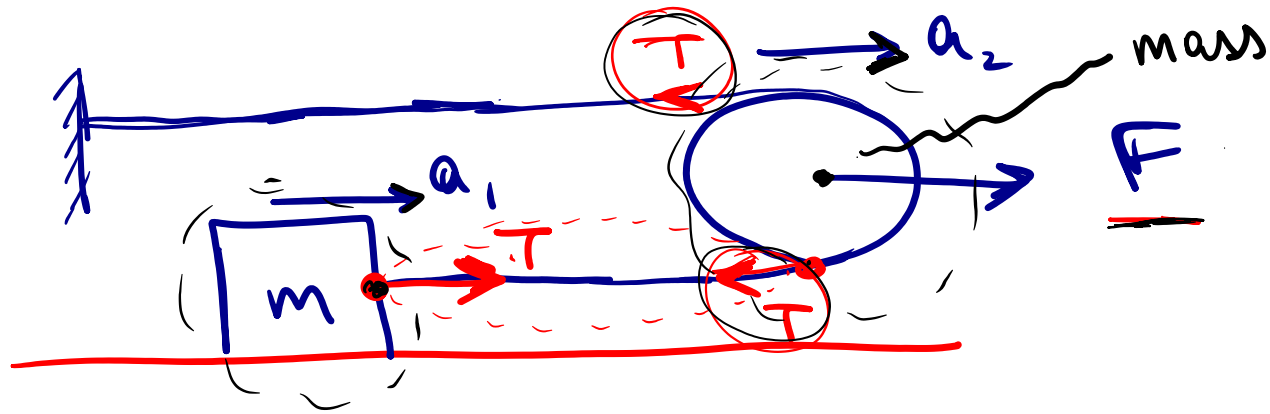


$$2mg - T' = 2ma_3$$

$$\underline{\underline{T \cdot a_1 + T' \cdot a_2 + T' \cdot a_3 = 0}}$$

$$2T' a_1 + -T' a_2 - T' a_3 = 0$$

$$\underline{\underline{2a_1 = a_2 + a_3}}$$



IMPORTANT POINTS

- 1) Same string \rightarrow Tension is the same
- 2) Tension is always pulling

$$m = 0$$

$$\sum F = 0$$

A free body diagram of a point on the string, showing two tension forces T pulling in opposite directions.

$$\sum \vec{T} \cdot \vec{a} = 0$$

$$-2Ta_2 + Ta_1 = 0$$

$$a_1 = 2a_2$$

